

# ANALYSIS AND IMPROVEMENT OF VALIANT ROUTING IN LOW- DIAMETER NETWORKS

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With support from:



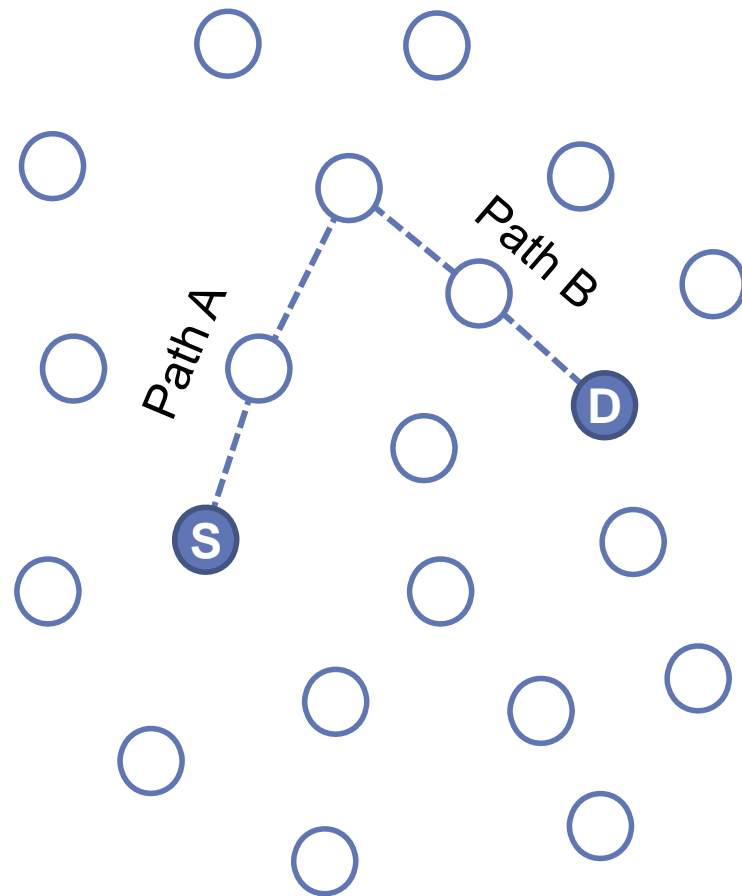
4th IEEE International Workshop of High-Performance Interconnection  
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Vienna, Austria, 24-Feb, 2018.

# Index

1. Background and motivation
2. Improvements to Valiant routing
3. Performance evaluation
4. Discussion and conclusions

# 1. Background and motivation

- Valiant routing
  - Randomized Routing mechanism originally proposed by Leslie Valiant for Hypercubes in [1] and square mesh, d-way shuffle and shuffle-exchange graphs networks in [2] .
  - Diverts traffic to an intermediate router
  - Double path length on average wrt minimal routing
  - Bounded worst-case permutation time
  - *Oblivious*

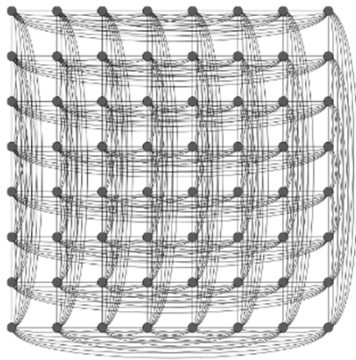


[1] L. Valiant, "A scheme for fast parallel communication," SIAM journal on computing, vol. 11, p. 350, 1982

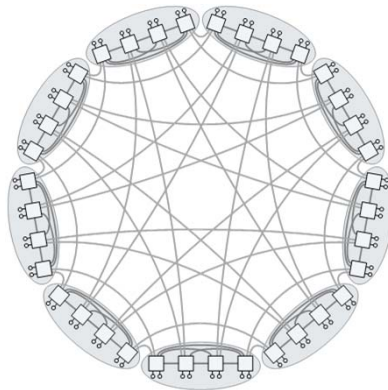
[2] L. G. Valiant, "Optimality of a two-phase strategy for routing in interconnection networks," IEEE Trans. Comput., vol. 32, no. 9, pp. 861–863, Sep. 1983.

# 1. Background and motivation

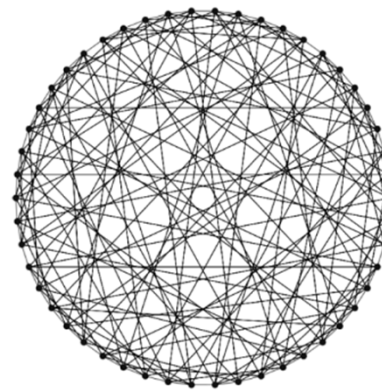
- Valiant has been used in low-diameter system networks
- Highly-scalable, low-cost topologies



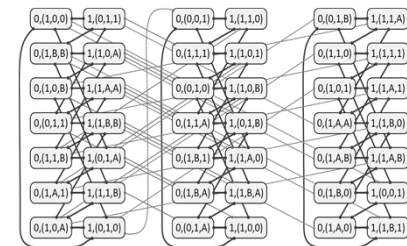
Flattened-Butterfly [3]



Dragonfly [4]



Slim Fly [5]



Projective Network [6]

- Low diversity of minimal paths
  - Concentration (multiple nodes per switch)
  - Valiant routing avoids such patterns of congestion
    - Often implemented as part of an adaptive routing mechanism.
- } Congestion-prone

[3] Kim, Dally, Abts. *Flattened Butterfly : A Cost-Efficient Topology for High-Radix Networks*. ISCA'07

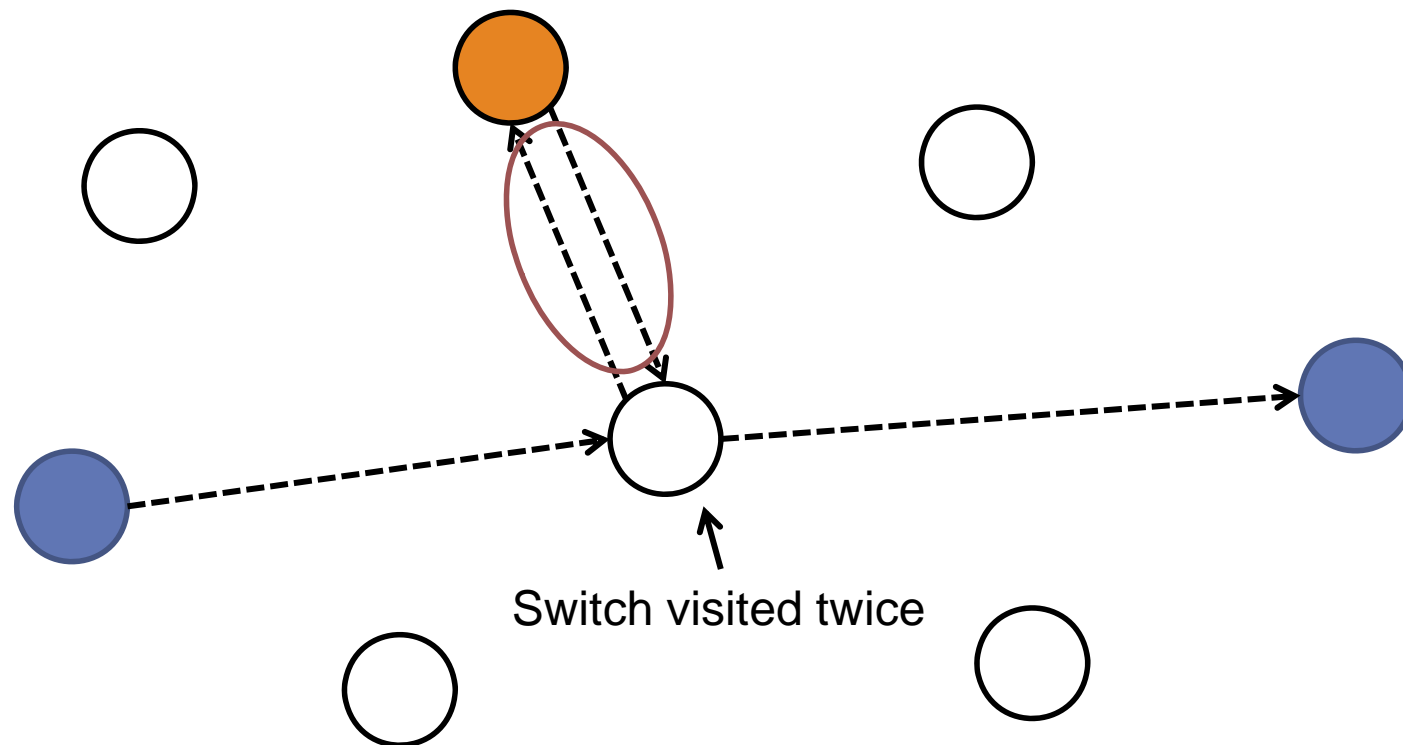
[4] Kim, Dally, Scott, Abts. *Technology-Driven, Highly-Scalable Dragonfly Topology*. ISCA '08

[5] Besta, Hoefler. *Slim Fly: A Cost Effective Low-Diameter Network Topology*. SC'14.

[6] Camarero, Martínez, Vallejo, Bevide. *Projective networks: Topologies for large parallel computer systems*. TPDS'17

# 1. Background and motivation

- Yébenes *et al.* [7] identified the *turnaround problem* when using Valiant routing in Slim Fly networks



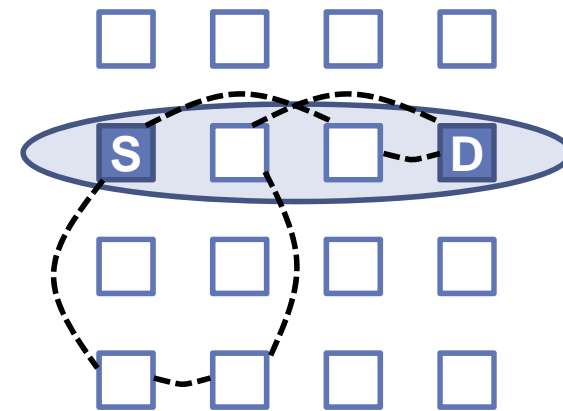
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1. Background and motivation
2. **Improvements to Valiant routing**
  1. Restricted intermediate router selection
  2. Path recomputation
3. Performance evaluation
4. Discussion and conclusions

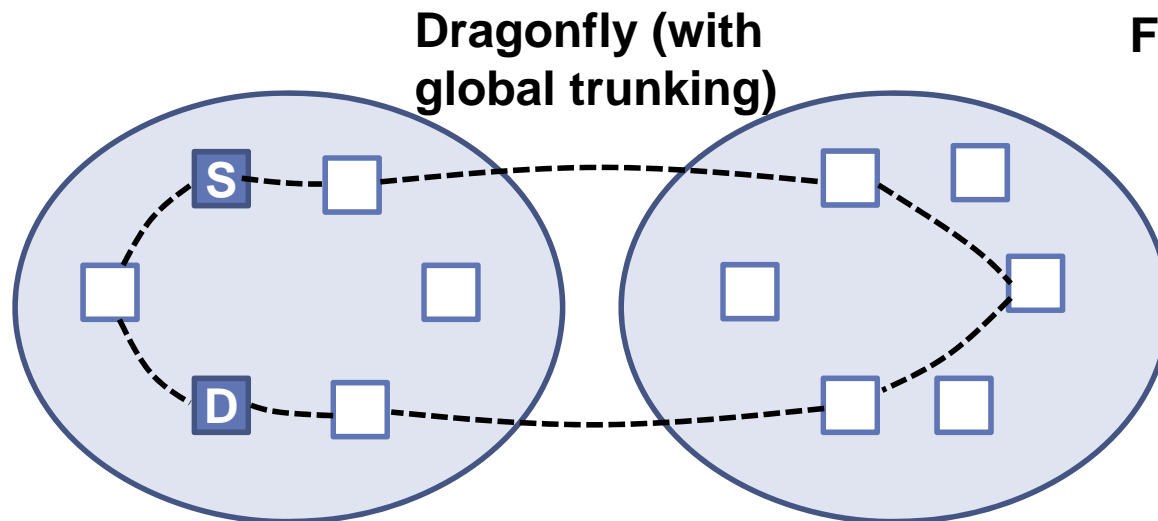
## 2. Improvements to Valiant Routing

### 2.1 Intermediate router selection

- A variant of the turn-around problem may occur without packets visiting switches twice.
  - Packets leave and return to a given network partition.



**Flattened Butterfly**

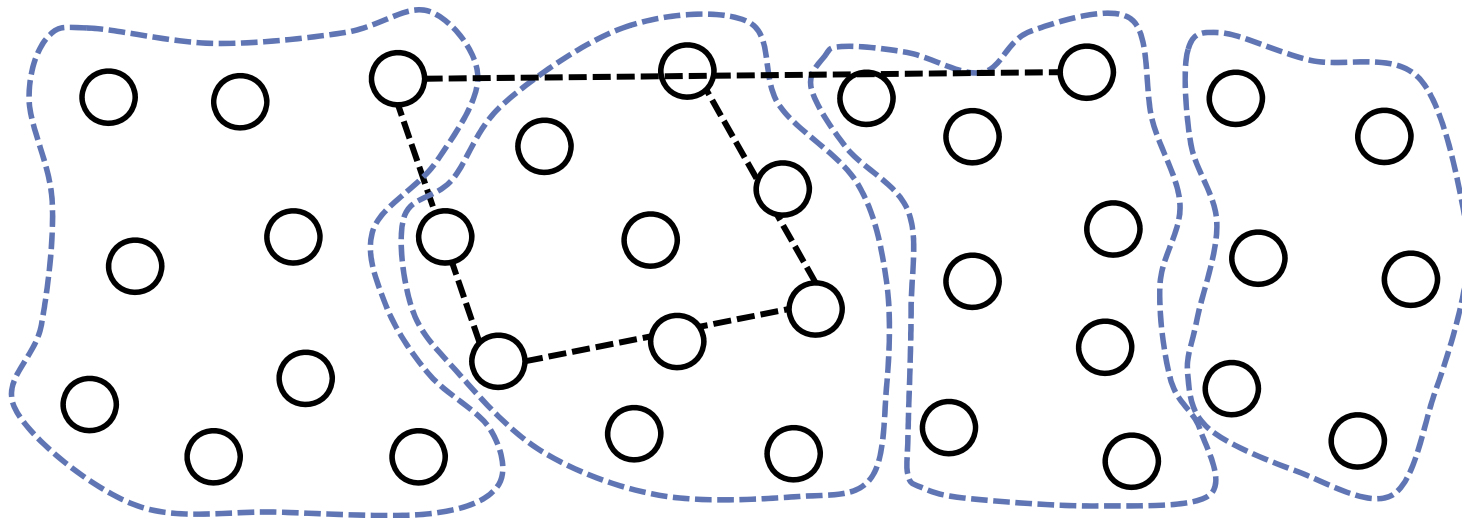


**Dragonfly (with  
global trunking)**

## 2. Improvements to Valiant Routing

### 2.1 Intermediate router selection

1. Determine network partitions
2. When both source & dest. nodes belong to the same partition
  1. Select intermediate node inside the partition
3. Otherwise
  1. Select intermediate node anywhere in the network.

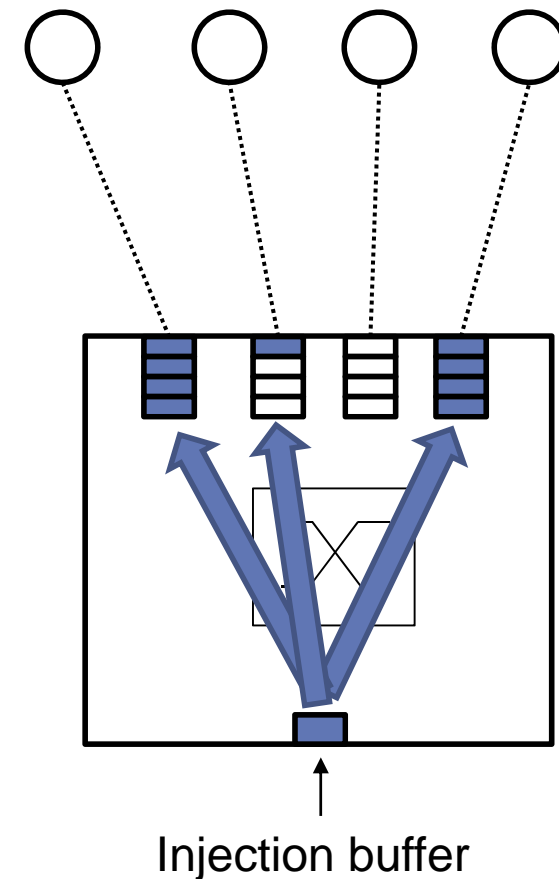




## 2. Improvements to Valiant Routing

### 2.2 Recomputation

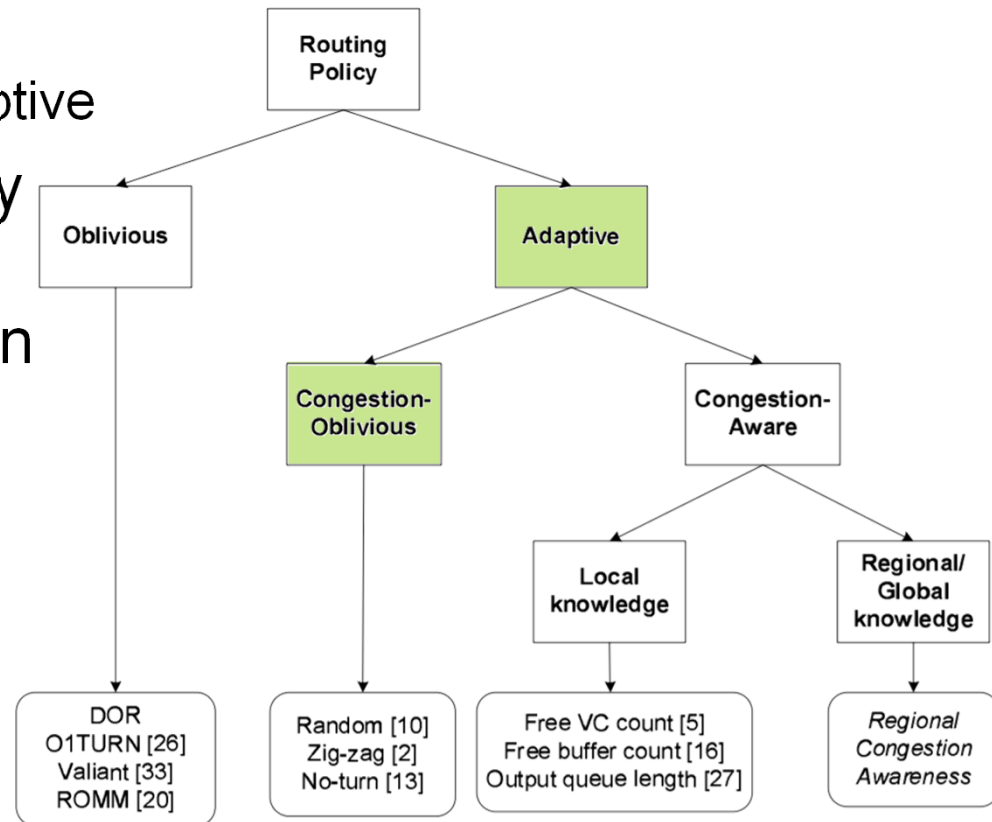
- Congestion situations may appear despite the randomization mechanism
  - Particularly when Valiant is used as part of an *adaptive* routing mechanism
- *Valiant with recomputation* makes a new intermediate node selection when the output port is not available



## 2. Improvements to Valiant Routing

### 2.2 Recomputation

- Valiant with Recomputation (VAL-Recomp) is no longer oblivious
  - But it is not completely adaptive
- According to the taxonimy by P. Graz *et al* in [8], Valiant with recomputation is *adaptive*, *congestion-oblivious*



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2. Improvements to Valiant routing
3. **Performance evaluation**
  1. Simulation setup
  2. Restricted Valiant
  3. Valiant with recomputation
  4. Impact of number of injection buffers
4. Discussion and conclusions

## 3. Performance evaluation

### 3.1 Simulation setup

- Dragonfly [4] network modelled using FOGSim [9]

Parameter	Value
Router size	23 ports (h=6 global, p=6 injection, 11 local)
Group size	12 routers, 72 computing nodes
System size	73 groups, 876 routers, 5,256 computing nodes
Latency (ns)	40/400 (local/global links), 200 (router pipeline)
Buffer size (KB)	100 KB (transit queues), 200 (injection buffers)
Router	2x frequency speedup, Virtual Cut-Through, iterative input-first separable allocator
Routing mechanisms	Minimal (MIN) Valiant (VAL) Restricted Valiant (RVAL) Valiant-Recomp (VAL-Recomp) Restricted Valiant-Recomp (RVAL-Recomp)

#### Topology

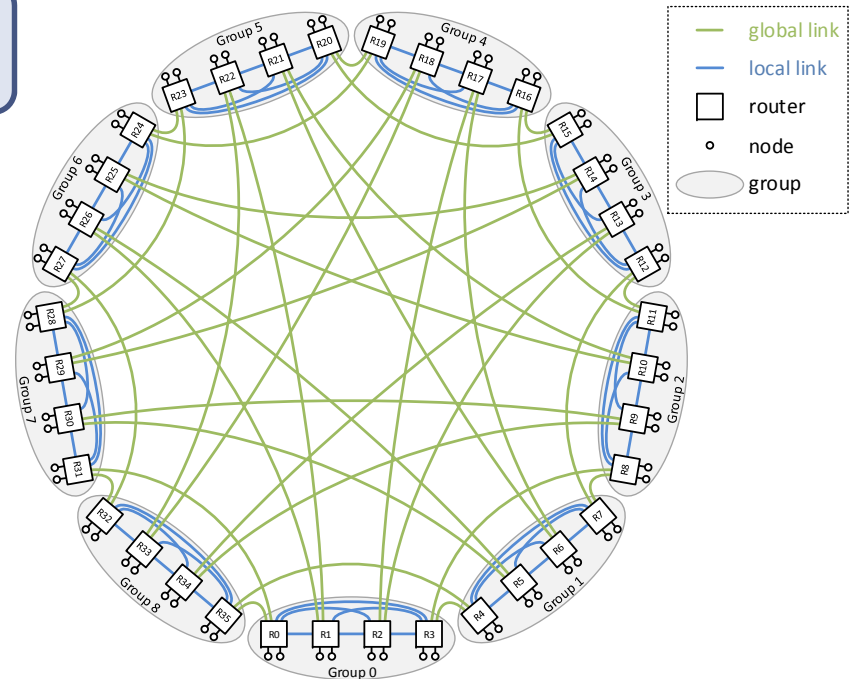
Uniform traffic

Adversarial traffic

Adv-local traffic

Hot-Region traffic

Permutation traffic

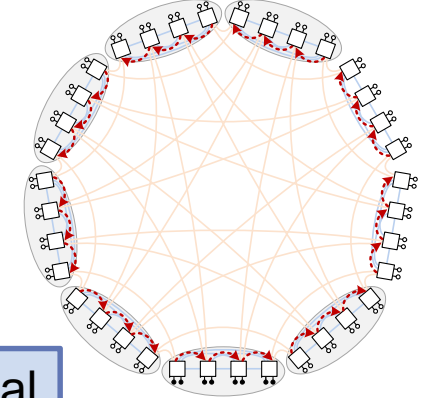
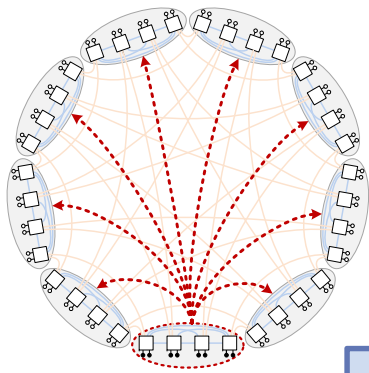


Strict permutation: No endpoint congestion  
Random: pattern differs for each simulation, but is fixed during each simulation

[4] Kim, Dally, Scott, Abts. *Technology-Driven, Highly-Scalable Dragonfly Topology*. ISCA '08

[9] García et al., *FOGSim Interconnection Network Simulator*, <http://fuentesp.github.io/fogsim/>

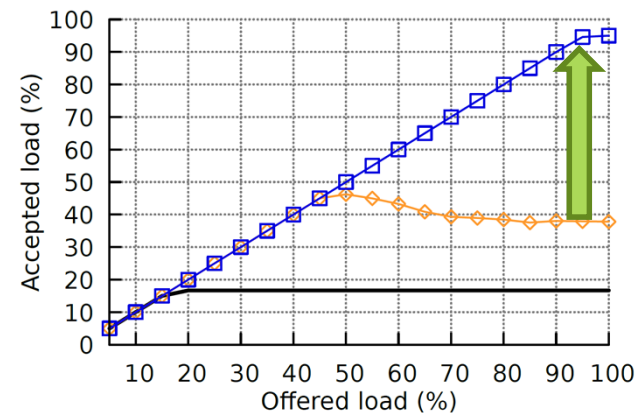
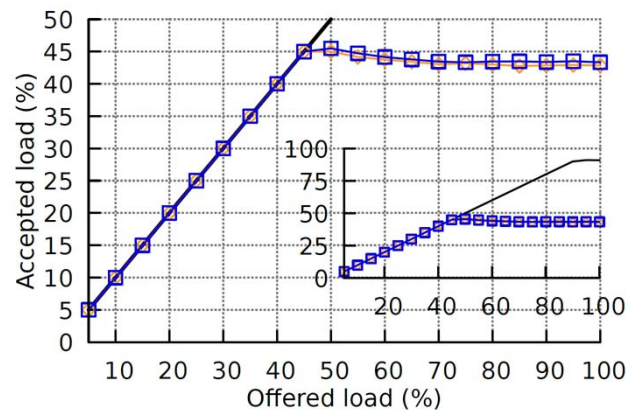
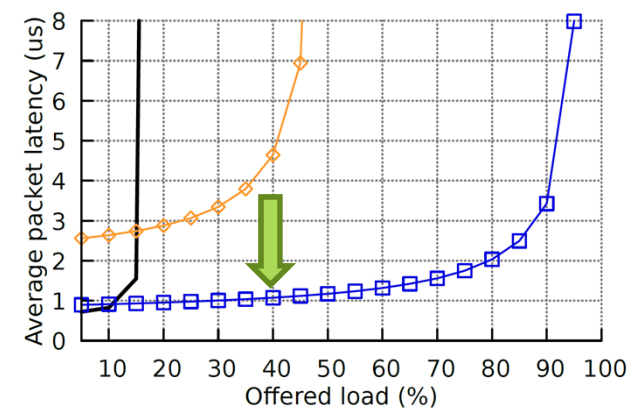
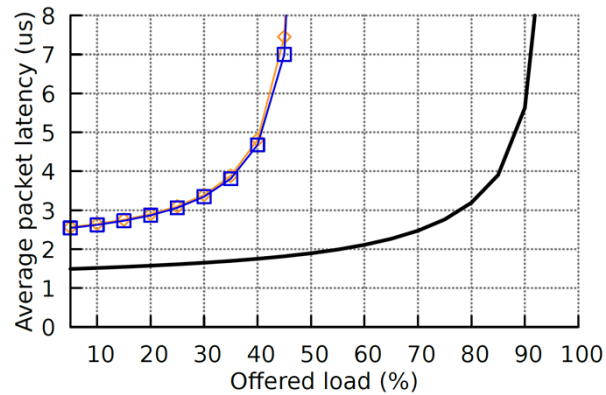
## 3.2 Restricted Valiant (RVAL)



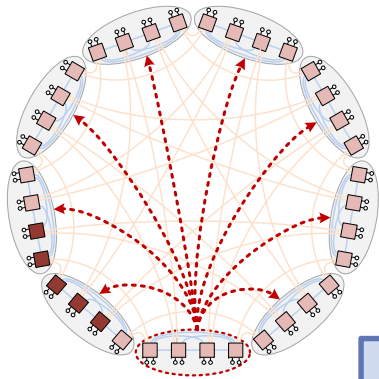
MIN — VAL — RVAL —

Random Uniform

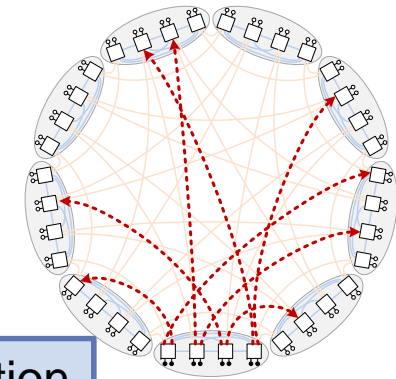
Adversarial-local



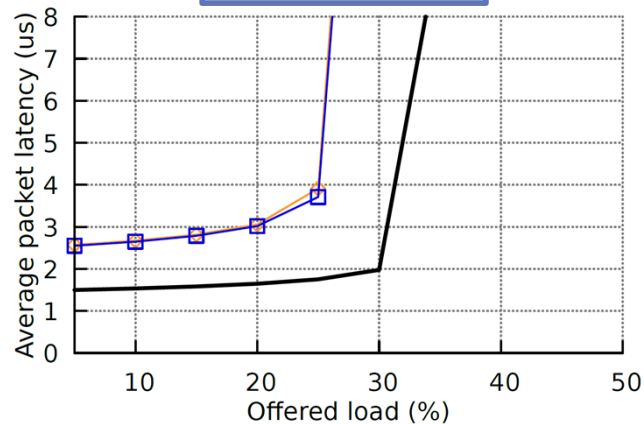
## 3.2 Restricted Valiant (RVAL)



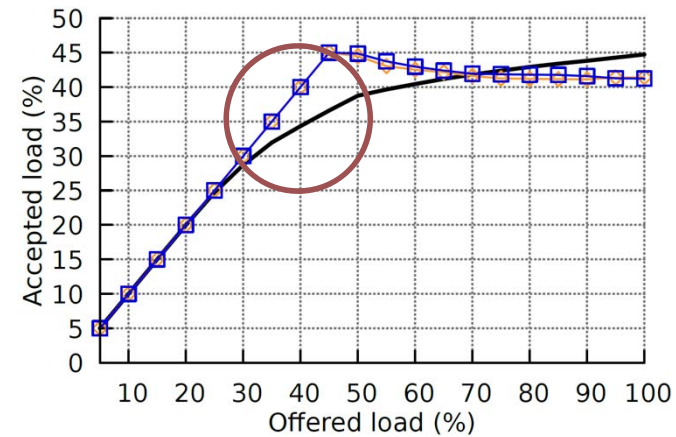
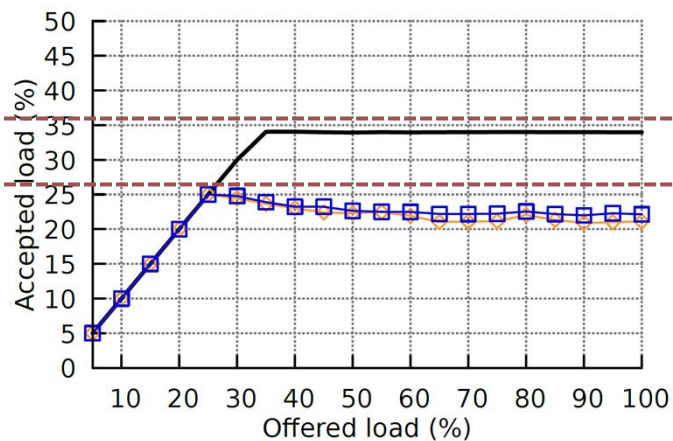
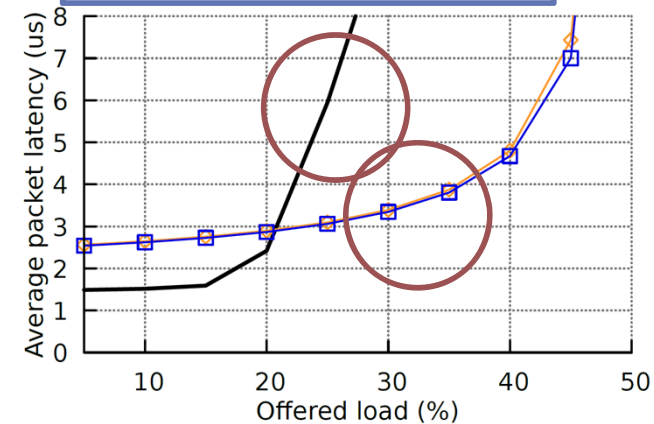
MIN — VAL —◇— RVAL —□—



Hot-Region

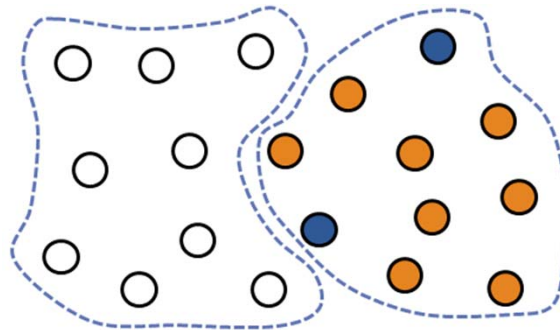


Random permutation



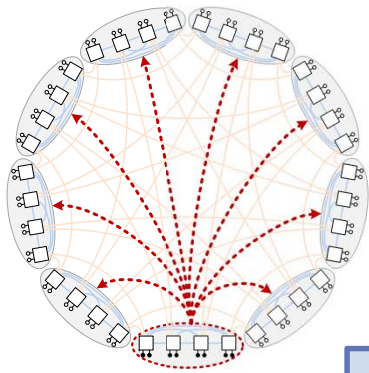
## 3.2 Restricted Valiant (RVAL)

- Partial conclusions:
  - **Restricted Valiant** in the Dragonfly is **highly beneficial** for intra-group traffic (Adversarial-local)
  - Very small benefit (no penalty) in other cases (~1%).



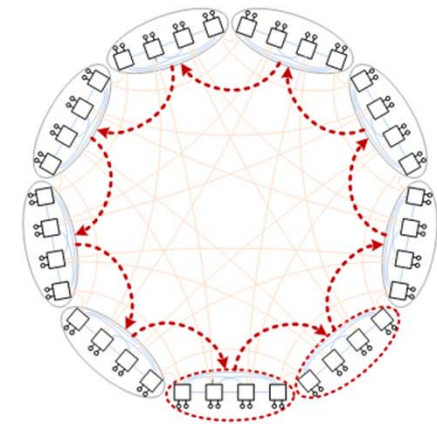
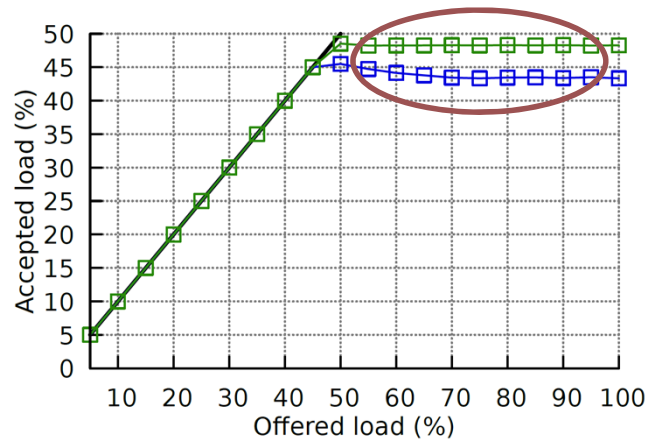
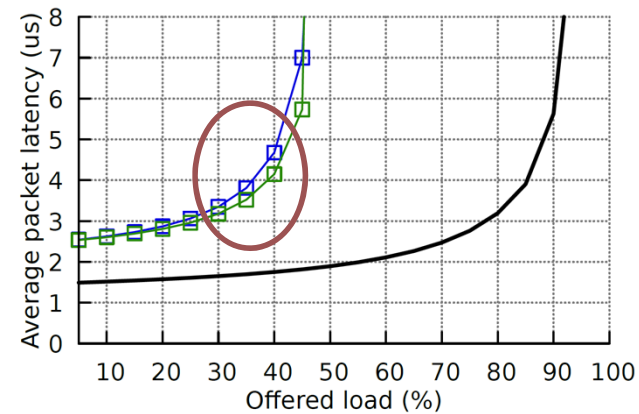


### 3.3 Valiant with recomputation

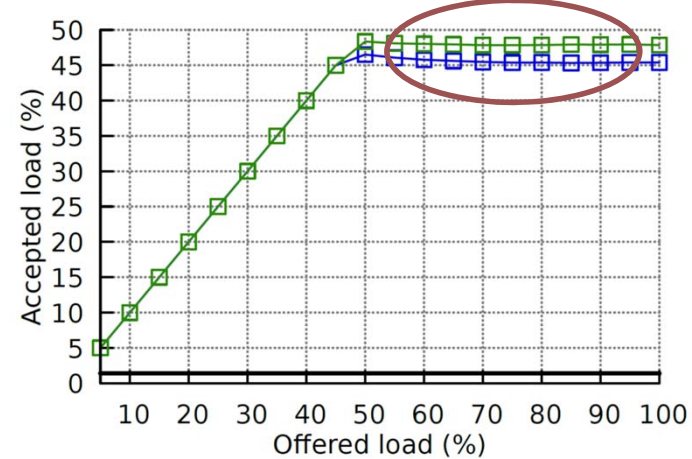
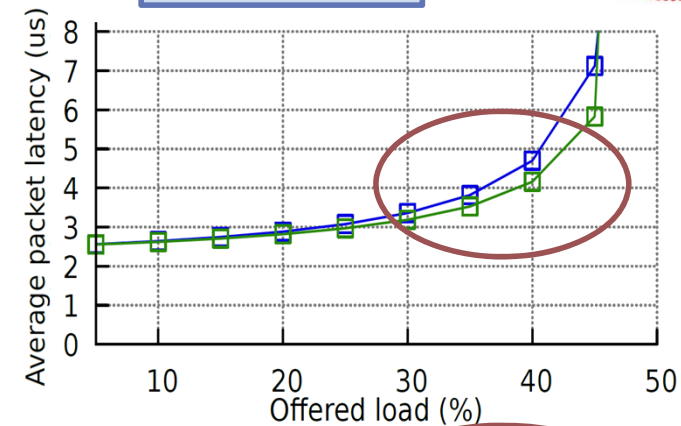


MIN — RVAL —□— RVAL-Recomp —□—

Random Uniform

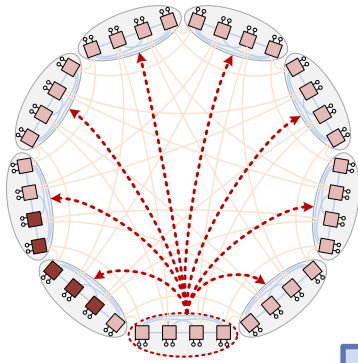


Adversarial

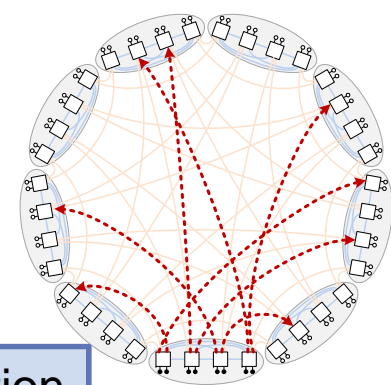




# 3.3 Valiant with recomputation

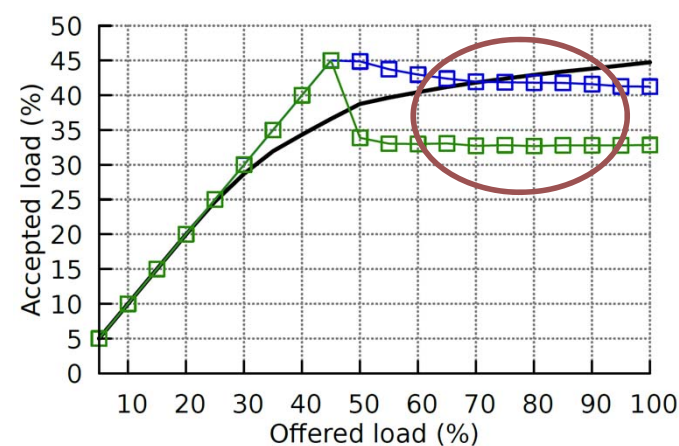
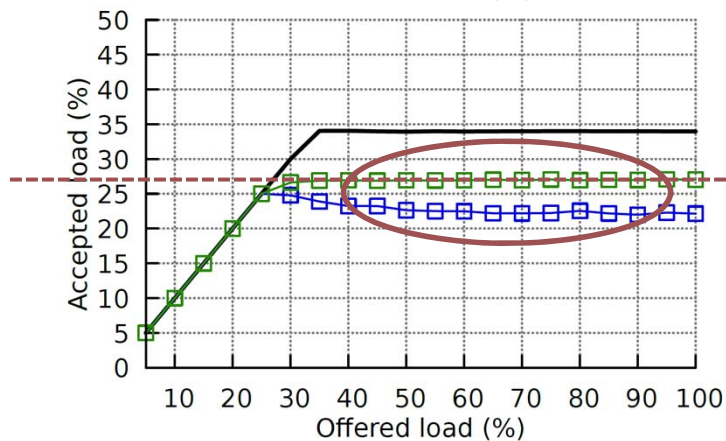
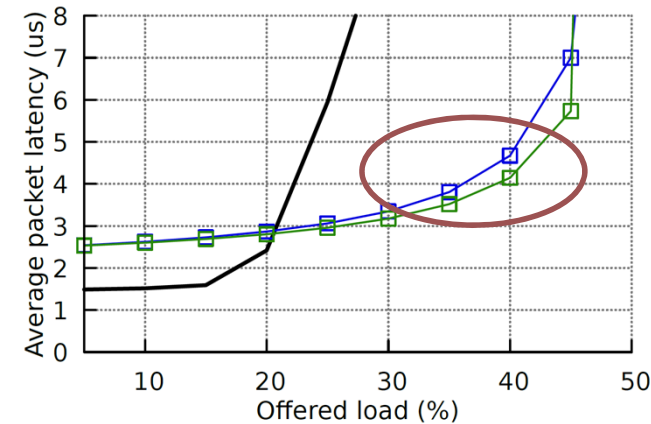
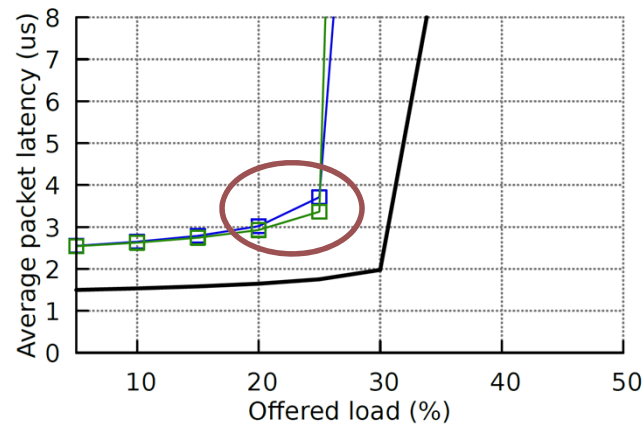


Hot-Region



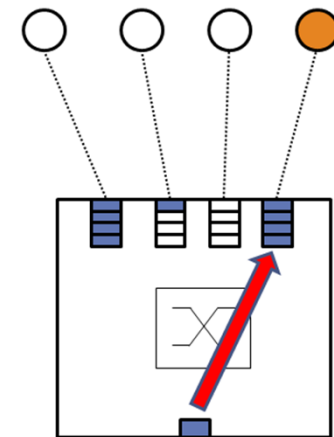
Random permutation

MIN — RVAL — RVAL-Recomp —











## 3.3 Valiant with recomputation

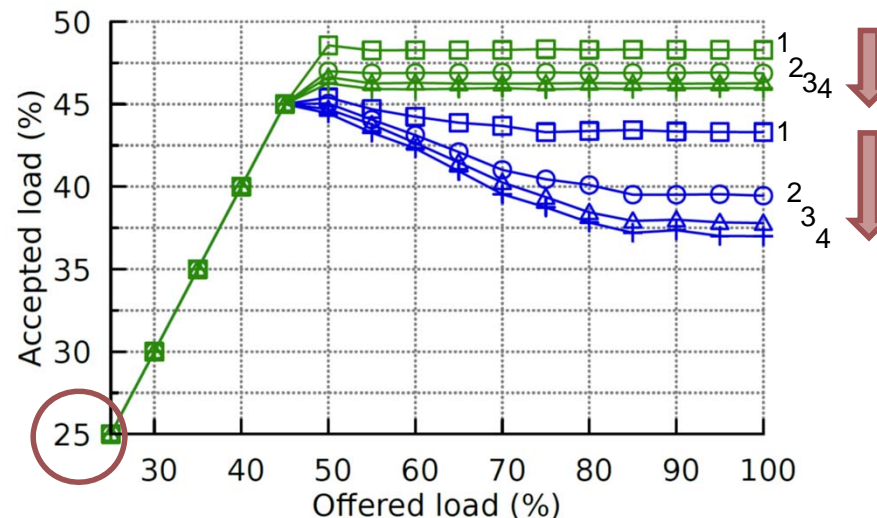
- Partial conclusions:
  - Valiant with recomputation **improves**:
    - **Stability** of the results (much less oscillations)
    - **Latency** before saturation
    - **Peak throughput**
  - The recomputation mechanism is **negative for random permutations of traffic in the saturation regimen**
    - It increases congestion issues after saturation



## 3.4 Number of injection buffers

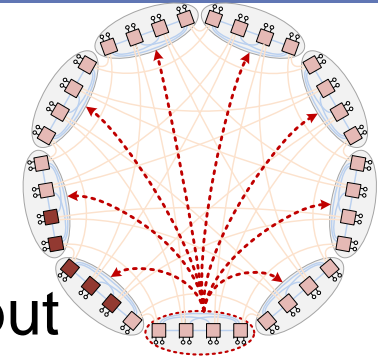
- When multiple buffers are used:
  - No significant difference for latency before saturation
  - Traffic injection after saturation increases with the number of buffers, what increases congestion
  - Typical behavior for 1-4 buffers under UN or ADV traffic:









RVAL - 1 Inj. buffer(s)      
 RVAL - 3 Inj. buffer(s)      
 RVAL-Recomp - 1 Inj. buffer(s)      
 RVAL-Recomp - 3 Inj. buffer(s)   
 RVAL - 2 Inj. buffer(s)      
 RVAL - 4 Inj. buffer(s)      
 RVAL-Recomp - 2 Inj. buffer(s)      
 RVAL-Recomp - 4 Inj. buffer(s) 

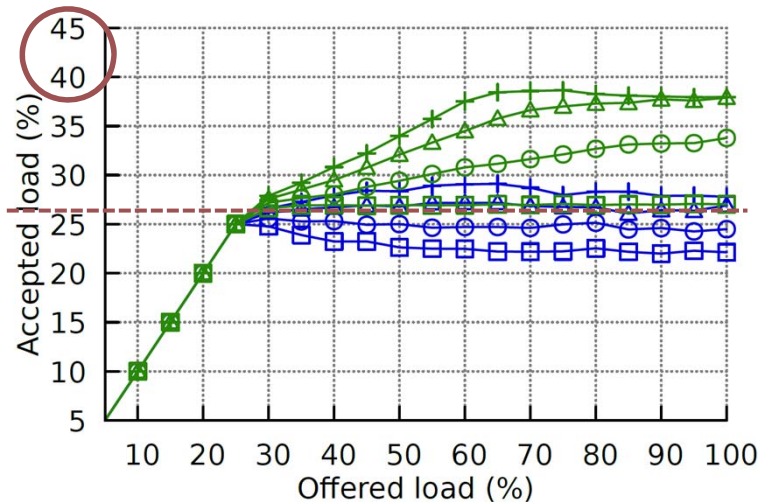


## 3.4 Number of injection buffers

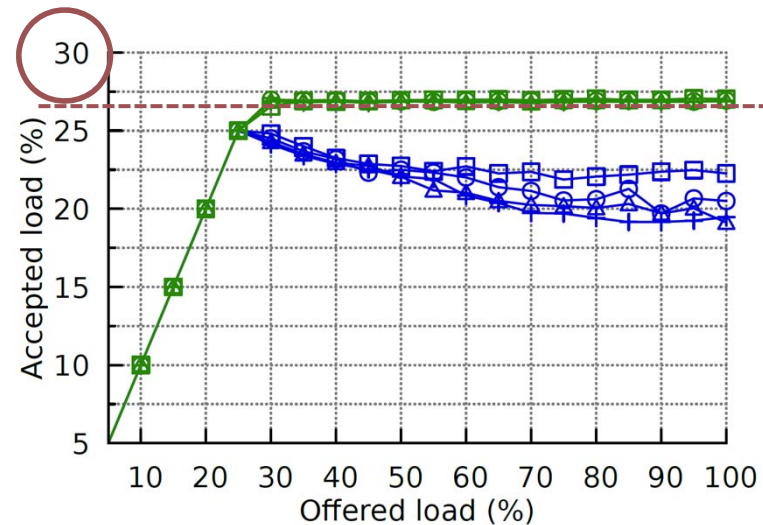
- Hot-región traffic: more buffers increase throughput with a DEST policy.



RVAL - 1 Inj. buffer(s)       RVAL - 3 Inj. buffer(s)       RVAL-Recomp - 1 Inj. buffer(s)       RVAL-Recomp - 3 Inj. buffer(s)   
 RVAL - 2 Inj. buffer(s)       RVAL - 4 Inj. buffer(s)       RVAL-Recomp - 2 Inj. buffer(s)       RVAL-Recomp - 4 Inj. buffer(s) 



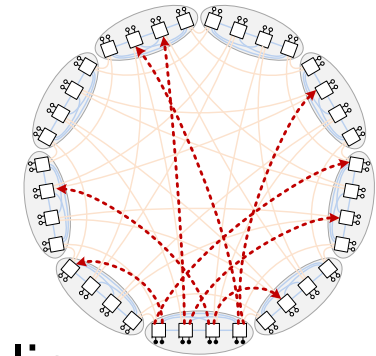
DEST policy: injection buffer selected by destination







RANDOM policy: injection buffer selected randomly, between available



## 3.4 Number of injection buffers



- **Random-permutation traffic:** more buffers severely increase congestion with a RANDOM policy

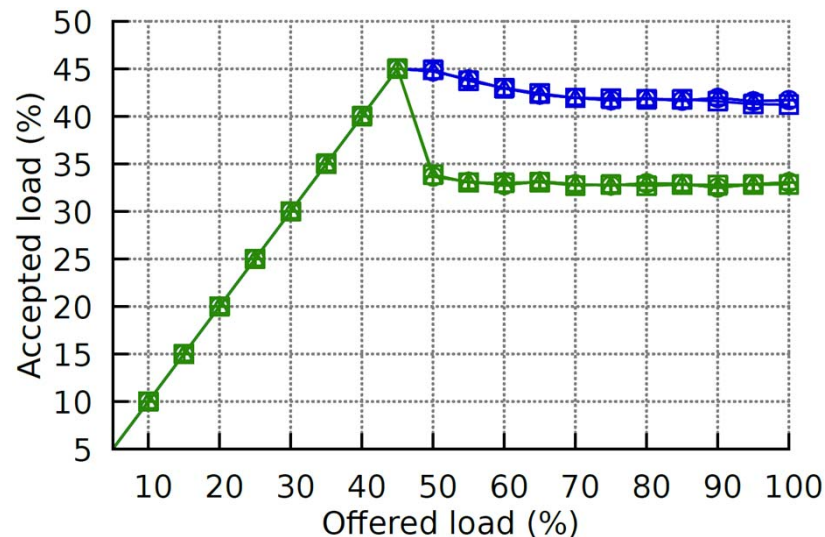


RVAL - 1 Inj. buffer(s)   
 RVAL - 2 Inj. buffer(s) 

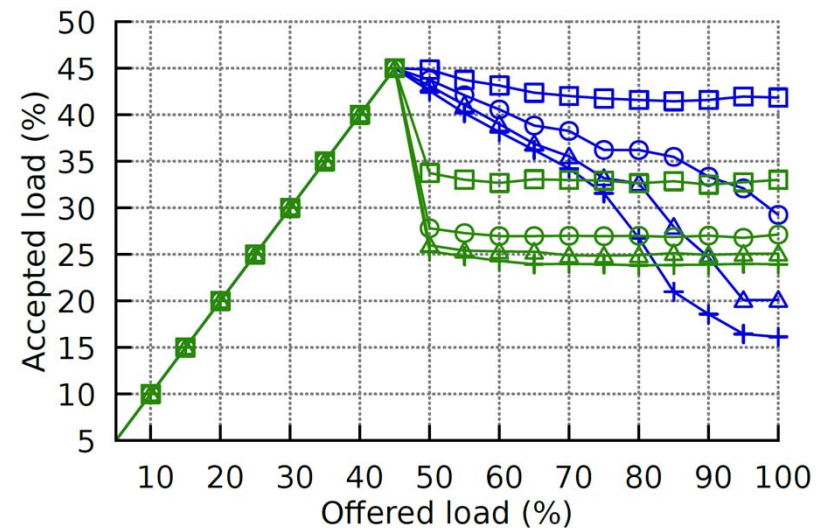
RVAL - 3 Inj. buffer(s)   
 RVAL - 4 Inj. buffer(s) 

RVAL-Recomp - 1 Inj. buffer(s)   
 RVAL-Recomp - 2 Inj. buffer(s) 

RVAL-Recomp - 3 Inj. buffer(s)   
 RVAL-Recomp - 4 Inj. buffer(s) 



DEST policy: injection buffer selected by destination



RANDOM policy: injection buffer selected randomly, between available



## 3.4 Number of injection buffers

- Partial conclusions:
  - Increasing the number of injection buffers increases the amount of injected traffic.
    - Increased congestion under UN, ADV and PERM
    - Reduces endpoint-congestion effect under HOT-REGION (traffic with endpoint congestion) with a per-destination buffer selection policy.

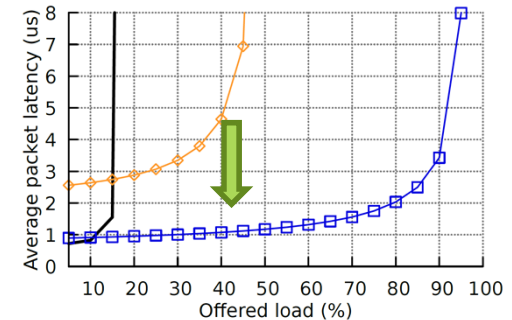
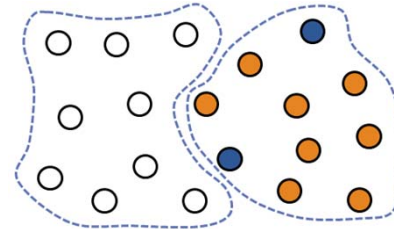
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## 4. Conclusions and future work

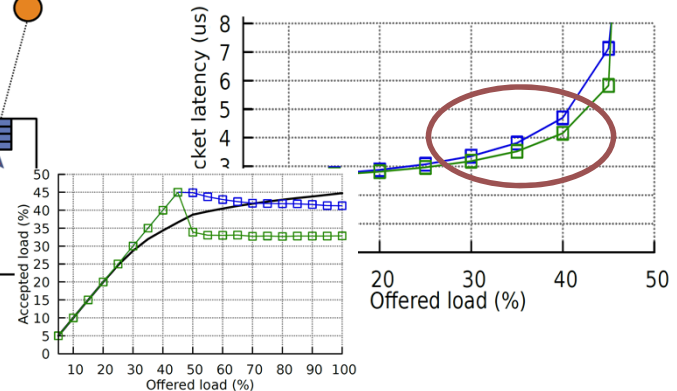
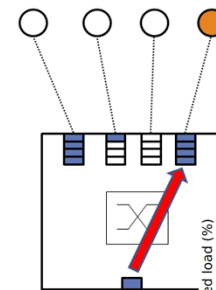
### • Restricted Valiant

- The performance improvement is dramatical for traffic internal to a partition (a Dragonfly group).



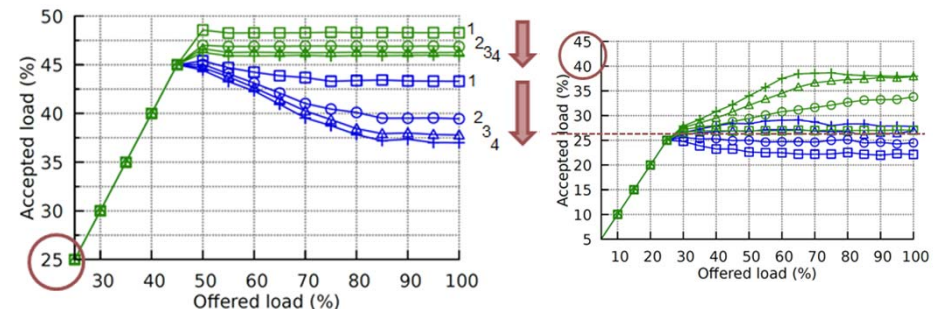
### • Valiant with recomputation improves the stability of the results, latency and peak throughput.

- More throughput also increases congestion



### • Number of virtual channels:

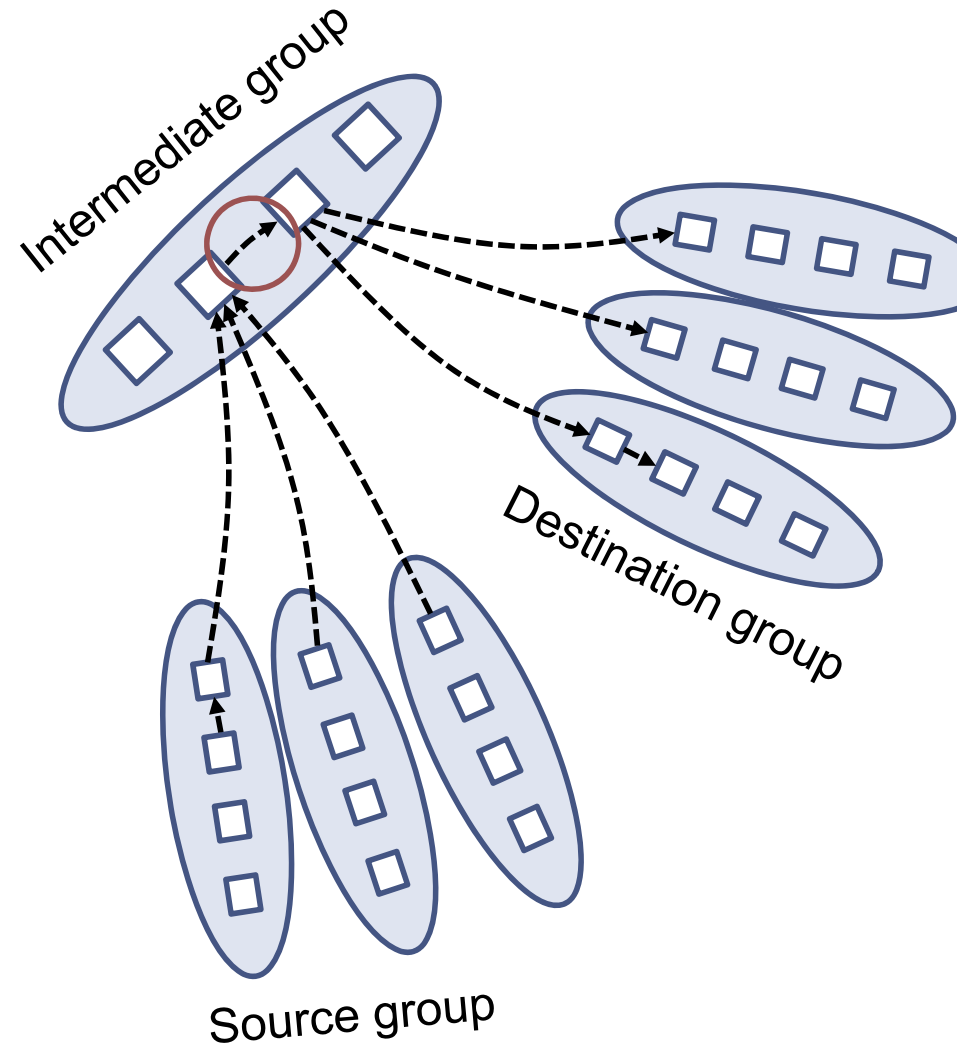
- More injection channels increase congestion
- HoLB reduction is effective in cases of endpoint congestion (Hot-Region traffic)





## 4. Conclusions and future work

- Our proposal for Restricted Valiant relies on *network partitions*.
  - *How to specify useful partitions for a given (nontrivial) topology?*
- How to define (proof) when the behavior of Restricted Valiant is “correct”?
  - Example: Restricted Valiant in the Dragonfly proposed by Kim *et al* in [4]
    - Denoted *Valiant-global* in [10]
    - Pathological performance under adversarial traffic identified in [11]
  - L. Valiant studies the *consumption time of a worst-case permutation*.
    - Should we use this analysis?
    - Is this equivalent to minimum throughput at saturation (per router)?



[4] Kim, Dally, Scott, Abts. *Technology-Driven, Highly-Scalable Dragonfly Topology*. ISCA '08

[10] J. Won, G. Kim, J. Kim, T. Jiang, M. Parker and S. Scott, "Overcoming far-end congestion in large-scale networks," HPCA'15

[11] M. García *et al*: "On-the-fly adaptive routing in high-radix hierarchical networks," IPDPS'12

## 4. Conclusions and future work

- **Other issues** we are exploring:
  - How does Restricted Valiant and Valiant with Recomputation behave when using **adaptive routing**?
  - How should we implement them in an interconnect that implements **table-based routing**?

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